Supplementary Appendix 1: Lifetable equations

The size of the MSM population of each age not previously diagnosed with HIV in each year was defined by the equation:

$$M_{a,t} = N_{a,t} * P_{msma} * Q_{a,t}$$

The proportion of the MSM population without an HIV diagnosis was defined by:

$$Q_{a,t+1} = Q_{a,t}^*(1 - D_{a,t} / M_{a,t})$$

Where:

 $M_{a,t}$ = Number MSM at risk in population of age a at year t

 $N_{a,t}$ = Number of men age a at year t

P_{msma} = Proportion of men age a who are MSM

Q_{a,t} = Probability of being free of HIV at age a and year t;

 $Q_{a,t}$ = 1.0 for all a < 18 and for all t < 1982

D_{a,t} = Number of new HIV diagnoses at age a and year t

The model assumed that in- and out-migration of MSM from each area did not vary by HIV status.