## Supplementary Appendix 1: Lifetable equations

The size of the MSM population of each age not previously diagnosed with HIV in each year was defined by the equation:
$M_{a, t}=N_{a, t} * P_{\text {msma }}{ }^{*} Q_{a, t}$
The proportion of the MSM population without an HIV diagnosis was defined by:
$Q_{\mathrm{a}, \mathrm{t}+1}=\mathrm{Q}_{\mathrm{a}, \mathrm{t}}{ }^{*}\left(1-\mathrm{D}_{\mathrm{a}, \mathrm{t}} / \mathrm{M}_{\mathrm{a}, \mathrm{t}}\right)$

Where:
$\mathrm{M}_{\mathrm{a}, \mathrm{t}}=$ Number MSM at risk in population of age a at year t
$N_{a, t}=$ Number of men age a at year $t$
$P_{\text {msma }}=$ Proportion of men age a who are MSM
$\mathrm{Q}_{\mathrm{a}, \mathrm{t}}=$ Probability of being free of HIV at age a and year t ;
$\mathrm{Q}_{\mathrm{a}, \mathrm{t}}=1.0$ for all $\mathrm{a}<18$ and for all $\mathrm{t}<1982$
$D_{a, t}=$ Number of new HIV diagnoses at age a and year $t$

The model assumed that in- and out-migration of MSM from each area did not vary by HIV status.

